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Research Article

# A Study on the Reduction of Drag and Heat Transfer on a Conventional Hypersonic Nose Cone

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ABSTRACT

In the present study, the effect of jet injection on two geometries—single-cone and double-cone—subjected to hypersonic flow is investigated. The simulations are performed using ANSYS-Fluent software. The baseline case is one where the nose lacks injection. The single-cone nose is tested at Mach 6, and the double-cone nose at Mach 5.4. The results show that increasing injection pressure results in a drag coefficient reduction of 49.2% for the single-cone geometry and 62.7% for the double-cone geometry, compared to the baseline. Additionally, the heat flux decreases by 60% for the single-cone nose and 41.3% for the double-cone nose. Higher injection pressure leads to an increase in bow shock standoff distance upstream of both the single-cone and double-cone noses. Increasing injection temperature has minimal impact on the drag coefficient and pressure distribution on the surface of the single-cone nose but significantly reduces the Stanton number, thereby decreasing heat transfer and enhancing nose cooling. Increasing the injection diameter from zero to 5 mm in the single-cone nose results in a 23% reduction in drag coefficient, while for the double-cone geometry, increasing the diameter to 16.5 mm reduces the drag coefficient by 75.04%. Changing the fluid type from air to a gas mixture decreases the maximum Stanton number by 19.3%.



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# 1. Introduction

The high-altitude and high-speed flight of spacecraft has led to extensive research on the aerodynamics of flying bodies at hypersonic speeds. Hypersonic flow, typically characterized by a Mach number greater than 5, is associated with unique physical phenomena such as ionization, extreme wave drag, aerodynamic heating, and intense flow gradients. Among these, heat transfer and drag reduction are the most critical challenges to address. Drag control is primarily influenced by the aerodynamic design of the body, while aerodynamic heating is governed by flow turbulence and chemical reactions in the air. Although numerous studies have been conducted to calculate aerodynamic heating and wave drag in hypersonic regimes [1], computational limitations have restricted the exploration of unsteady hypersonic flow regimes. This paper focuses on the use of counterflow jet injection as a method to simultaneously reduce aerodynamic heating and drag force in hypersonic flows.

## 1.1. *Methods for Drag and Heat Flux Control*

Various methods have been proposed to control drag and heating in supersonic and hypersonic flows. These include thermal shields [2], aerospikes [3], jet injection [4, 5], cavities [6], energy discharge [7], and combined methods such as jet injection with cavities [8] or aerospikes with transverse gas injection [9]. Each method has its advantages and limitations. For instance, energy discharge effectively reduces drag but has minimal impact on heat flux reduction. Cavities are effective in controlling heat flux but may increase drag in certain scenarios. Thermal shields, while useful, are limited by their weight and operational duration. Aerospikes, though simple to install, suffer from rapid degradation at high temperatures. Among these, counterflow jet injection has emerged as a promising technique due to its potential to address both drag and heating challenges simultaneously.

## 1.2. *Counterflow Jet Injection: Mechanisms and Challenges*

Counterflow jet injection involves injecting a gas through a narrow channel on the body into the external flow. This method requires careful consideration of internal flow dynamics, including flow dilution [10, 11], proper mixing [12, 13] to control gas temperature, and nozzle design to achieve appropriate velocity, pressure, and temperature for injection [14, 15]. The external flow interaction with the injected jet is critical for achieving drag and heat flux reduction. Studies have shown that the effectiveness of counterflow jets depends on parameters such as jet diameter, pressure ratio, injected gas type, and free stream Mach number.

## 1.3. *Numerical and Experimental Studies on Counterflow Jets*

Numerous studies have investigated the performance of counterflow jets in hypersonic flows. Guo et al [16] studied the effects of opposing jet layout on a hypersonic flow passing a blunt body. They mentioned that in comparison with the no jet case, the counter jet pushes the detached shock wave upstream greatly. The oblique jet layout also can push the detached shock wave upstream for a long distance, and two jet layers are generated symmetrically in the flow field. Huang et al. [17] demonstrated that increasing the jet diameter decreases the critical pressure ratio, while larger body diameters improve temperature control efficiency. wang et al [18] show that a single pressure parameter can control the formation of a supersonic opposing jet to form a long penetration mode and a short penetration mode. The ratio of the ambient pressure to the jet pressure at the stagnation point of the blunt body can directly affect the flow field structure of the opposing jet, and reasonable control of opposing jet parameters is an effective way for thermal protection and drag reduction of blunt body structures. Jin [19] found that counterflow jets perform better at higher free stream Mach numbers, particularly under lower pressure ratios. Yuan et al. [20] highlighted the importance of jet exit velocity, showing that a velocity of 200 m/s can reduce the heat transfer coefficient by up to 36%. Shen et al. [21] compared the effectiveness of different gases, with helium achieving the highest efficiency (85.1%) in reducing aerodynamic heating. Gao et al. [5] confirmed that increasing jet pressure enhances penetration into the counterflow, thereby reducing surface temperature. Li et al. [22] explored the effect of multiple jets, finding that increasing the number of jets (up to 9) significantly reduces aerodynamic heating and drag. Gorderodbari et al. [23] emphasized the role of injected gas type and pressure, noting that higher injection pressures improve cooling efficiency. Zhu and Ji [4] identified the critical jet pressure for maximum drag reduction (32.6%) at Mach 2.5. Yixing [24] introduced a dimensionless parameter combining mass flux and jet pressure ratio, showing a 20% drag reduction at Mach 3.98. Gardaroodbari et al. [25] compared helium and carbon dioxide, with helium proving more effective in reducing thermal load. Chen et al. [26] used LES to study jet penetration states, distinguishing between long and short

**Table 1.** Summary of Research Studies

| Ref. | year | $M_\infty$ | $M_j$ | $T_{0,j}(K)$ | $AOA$ (deg) | gas | Geometry layout | Numerical Simulation | experimental | Drag Reduction | Heat Flux Reduction |
|---|---|---|---|---|---|---|---|---|---|---|---|
| [16] | 2019 | 6 | 1.5 | 300 | 0 | Air | Hemisphere | ■ | □ | ■ | ■ |
| [17] | 2019 | --- | 1 | --- | 0 | --- | Hemisphere and Cone | ■ | □ | □ | ■ |
| [18] | 2019 | 10 | --- | 300 | 0 | Nitrogen | Apollo | ■ | □ | □ | ■ |
| [19] | 2019 | 6 | 1 | 300 | 0 | Air | Hemisphere | ■ | □ | □ | ■ |
| [5] | 2018 | --- | --- | --- | 0 | Air | Hemisphere | ■ | □ | □ | ■ |
| [20] | 2016 | 6 | 1 | 300 | 0 | Air | Wave Rider | ■ | □ | ■ | ■ |
| [21] | 2015 | 9.5 | 1 | 300 | --- | ---- | Blunt Nose Cone | ■ | □ | □ | ■ |
| [4] | 2014 | 5.2 | 1 | --- | --- | Air | Hemisphere | ■ | □ | ■ | □ |
| [22] | 2013 | 3.98 | 1 | 300 | 0 | N2 | Hemisphere | ■ | □ | ■ | □ |
| [23] | 2012 | 5.75 | 1 | 300 | 0 | ---- | Reentry Capsule | ■ | □ | □ | ■ |
| [24] | 2011 | 2.5 | --- | 294 | 0 | Air | Hemisphere | ■ | □ | ■ | □ |
| [25] | 2011 | 6.5 | 1 | 300 | --- | Air | Ogive Nose | ■ | □ | ■ | ■ |
| [26] | 2011 | 5.8 | --- | --- | 0 | --- | Hemisphere | ■ | □ | ■ | ■ |
| [27] | 2010 | --- | 1 | 300 | 0 | --- | Two Geometries | ■ | □ | ■ | ■ |
| [28] | 2009 | 8 | --- | --- | 0 | --- | Reentry Capsule | □ | ■ | □ | ■ |
| [29] | 2009 | 8 | --- | --- | 0 | --- | Reentry Capsule | □ | ■ | ■ | □ |
| [30] | 2009 | 5.9 | --- | --- | 0 | --- | Reentry Capsule | □ | ■ | □ | ■ |
| [31] | 2007 | --- | --- | 300 | 0,10 | --- | Apollo | ■ | □ | ■ | ■ |

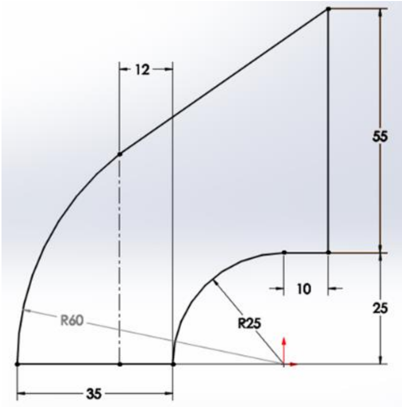
penetration modes based on pressure ratios. Anjalidowi and Aruna [27] examined critical jet parameters at Mach 5.6, observing that increasing jet pressure reduces frictional drag, total drag, and heat transfer. Shah et al. [28] categorized jet structures into four regions based on pressure ratios, highlighting the transition between short and long penetration states. Tamada et al. [29] compared supersonic and hypersonic flows, showing that short penetration occurs at lower pressure ratios in hypersonic regimes. Kulkarni and Reddy [30, 31] experimentally demonstrated significant heat transfer reduction (45%) and drag reduction with increasing jet pressure ratios. Sreeram and Jagadesh [32] found that heavier gases like nitrogen reduce heat transfer more effectively near the stagnation point, while helium performs better farther from it. Cheng et al. [33] showed that counterflow jets lose effectiveness at non-zero attack angles.

### 1.4. *Critical Analysis and Research Gaps*

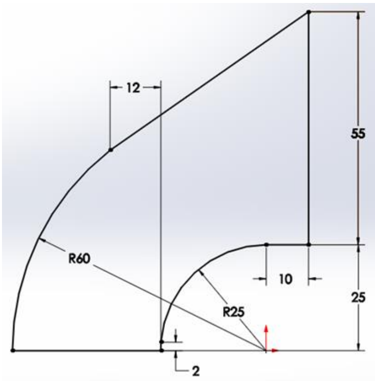
While significant progress has been made in understanding counterflow jet dynamics, several gaps remain. For instance, the transition between jet-off and jet-on states, flow field oscillations, and the stability of jet structures at varying pressure ratios require further investigation. Additionally, the combined effects of multiple jets and the influence of different gas types on jet penetration and cooling efficiency need deeper exploration. The present study aims to address some of these gaps by focusing on the external flow interaction of counterflow jets and their simultaneous impact on drag and heat flux reduction. Table 1 summarizes the aforementioned studies. In the present article, the geometry and numerical model are first described. Then, the validation of the solution, mesh independence, and y+ examination are conducted. The next section investigates the effects of injection pressure ratio, jet diameter, injection temperature, and the type of injecting fluid within the computational domain. The changes in shock position, pressure distribution, temperature, and Mach number near the nose are examined. Subsequently, the geometry of the dual-conical configuration is analyzed in both non-injection and injection scenarios. In this context, the effects of jet diameter and injection pressure ratio on the flow characteristics near the nose, as well as the position and structure of the shock wave, are studied. In the conclusion section, a summary of the main achievements of the paper is presented, and suggestions for future work are proposed.

## 2. Geometry and Numerical Model

The two-dimensional geometric model used in this paper is shown in Figure 1. According to Figure 1 (a), the geometry consists of a quarter-circle nose with a radius of 25 mm, followed by an extension of 10 mm. In Figure 1 (b), the counterflow jet is installed in front of the blunted body, with a jet diameter of 2 mm. The selected geometry is adapted from reference [34].




a) Without Jet Injection




b) With Jet Injection

**Fig. 1.** Dimensions of the Solution Field [34]

The Mach number, static pressure, static temperature, and angle of attack for the free stream, along with the Mach number, stagnation pressure, and stagnation temperature for the counterflow jet, are presented in Table 2.

**Table 2.** Specifications of Free Stream and Jet

| Free stream conditions | Injection conditions | Wall conditions |
|---|---|---|
| Air | Nitrogen | $T_W$=295 K |
| $Ma_\infty$ = 3.98 | $Ma_j$ = 1 | No Slip |
| $P_{0\infty}$ = 1.37 MPa | PR= 0.2-0.8 | |
| $T_{0\infty}$ = 397 k | $T_{0j}$ = 300 k | |

The initial wall temperature is set to 300 K, and the airflow is considered as an ideal gas. Figure 2 shows the structured mesh generated using ICEM software and the boundary conditions. The boundary conditions include axis (axisymmetric), far-field, pressure outlet, and pressure inlet (counterflow jet boundary condition). The k-ω SST turbulence model is selected. In this paper, the Reynolds Averaged Navier Stokes (RANS) equations are solved to obtain heat load and drag coefficient values. The implicit AUSM scheme is used for flux calculation, which is suitable for capturing sharp gradients like shock waves in supersonic/hypersonic flows. Second-order spatial discretization accuracy is considered.

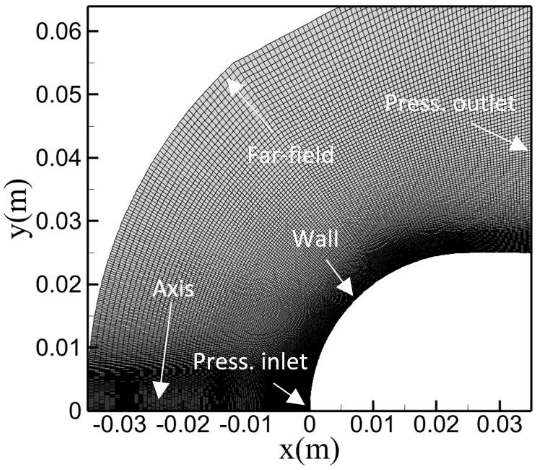
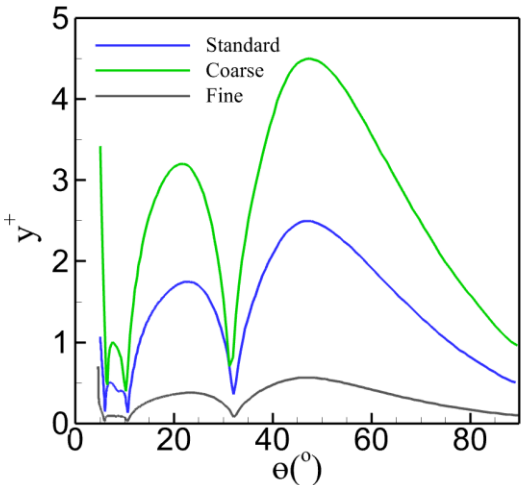



**Fig. 2.** Structured Mesh of the Computational Domain

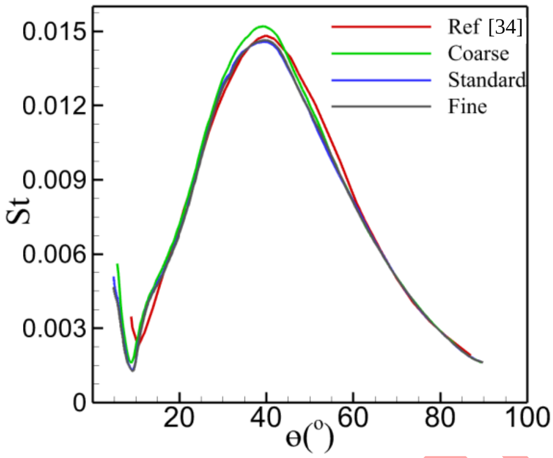
## 3. Validation and Grid Independence

### 3.1. *Grid Independence*

To ensure the accuracy of the numerical simulations, the study performs validation using a grid independence study. The grid independence study examines different mesh resolutions to ensure that further refinement does not significantly alter the results. For the validation model, three meshes were used: coarse, standard, and fine. The coarse mesh includes 27,200 cells, the standard mesh includes 80,876 cells, and the fine mesh includes 114,000 cells. To apply the boundary layer mesh on the model surface for increased accuracy, the height of the first cell is calculated to maintain a y+ value of around 3, and then the mesh is refined near the surface, especially close to the nose, to accurately simulate regions with high gradients. The y+ values for these three meshes are presented in Figure 3a. It can be observed that the y+ values for the standard and fine meshes are appropriate. The results for the Stanton number distribution on the surface under the mentioned flow conditions are presented in Figure 3b. Based on the graph, it is observed that the y+ results for the standard mesh do not differ significantly from the fine mesh. In other words, refining the mesh further does not change the results, indicating that the results obtained with the standard mesh are grid-independent. Therefore, the standard mesh with 70,876 cells will be used in the remainder of this paper.




a) The Range of y+ for Three Different Meshs




b) Variations of the Stanton Number on the Nose as a Function of the Angle θ

**Fig. 3.** y+ and Stanton number

## 3.2. *Validation*

Two parameters, drag force and aerodynamic heating, are very important in this research. Drag force is the result of pressure distribution on the surface and to study this parameter, pressure distribution on the surface has been studied under different conditions. Also, the heat flux generated on the surface is presented with Stanton number (St). Stanton number represents the heat flux generated on the surface. The Stanton number is a dimensionless parameter used to measure heat transfer between a surface and the surrounding fluid. It represents the ratio of convective heat transfer to thermal energy capacity in the fluid. In this paper, the Stanton number is used to evaluate the effectiveness of jet injection in reducing heat transfer on hypersonic nose geometries. Stanton number is calculated using the following formula:

$$\mathrm{St} = \frac{q_w}{(T_{aw} - T_{wall})\rho_\infty c_{p_\infty} u_\infty} \qquad (1)$$

In the above formula $q_w$ represents heat transfer, $\rho_\infty$ is the free stream density, $c_{p_\infty}$ is the specific heat capacity, $u_\infty$ is the free stream velocity , $T_{wall}$ is the wall temperature and $T_{aw}$ is the adiabatic wall temperature. Due to viscous dissipation (friction between adjacent layers of the fluid), a region with high temperature changes forms within the boundary layer. The high-temperature fluid within the boundary layer transfers heat to the body until the temperature gradient at the wall becomes zero. This temperature is called the adiabatic wall temperature $T_{aw}$ and is calculated using the following formula:

$$T_{aw} = T_\infty\{1 + \sqrt[3]{pr}[(\gamma - 1)/2]M_\infty^2\} \qquad (2)$$

In this relation, $T_\infty$ is the free stream temperature and $M_\infty$ is the free stream Mach number. The Prandtl number (pr) is 0.71. $\gamma$, the ratio of specific heats, is 1.4. The boundary conditions considered in this section are similar to those stated in reference [32]. Given the significant temperature variations in the flow field, the parameters Cp and k are considered as functions of temperature. Therefore, these parameters cannot be assumed constant and must change with temperature. The results for the Stanton number distribution on the surface, considering compressibility effects for both constant and temperature-dependent Cp and k, are shown in Figure 4 and compared with the reference [34]. For constant values of Cp and k, there are differences between the present study and the reference [34] in the range of 30 to 40 degrees. However, when Cp and k are considered variable, the results show excellent agreement.

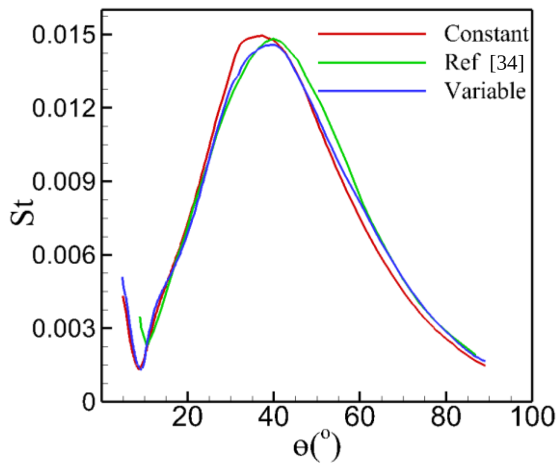


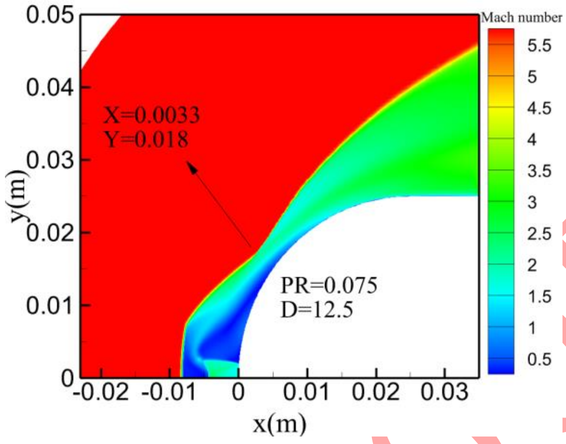

**Fig. 4**. Variations of the Stanton Number on the Nose as a Function of the Angle θ for Constant and Temperature-Dependent Values

## 4. Results

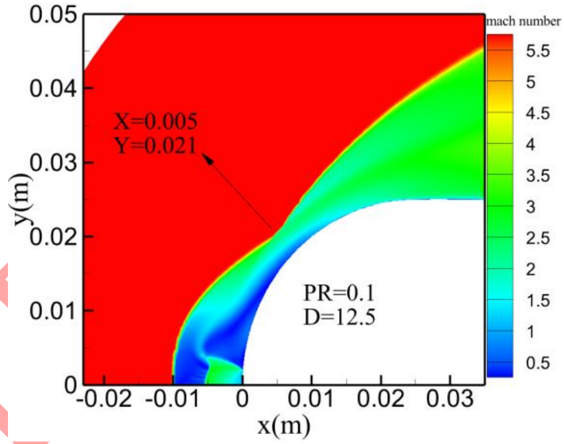
In this section, the results of the numerical simulation are examined. As stated in the previous sections, various parameters play a role in drag reduction and heat transfer, each of which will be analyzed in this section.

The most important parameter that has the greatest effect on drag reduction, based on studies, is the jet injection pressure ratio. The geometry under study is the same hemisphere geometry described in section 2 (Figure 1). The boundary conditions for the free stream are fixed with a Mach number $M_\infty=6$ stagnation pressure $P_\infty=4020$ kPa, and stagnation temperature $T_\infty= 1812$ K. Additionally, injection pressures of 301.5, 402, 603, 804, and 1005 kPa are considered to examine the jet injection pressure. In all these cases, the ratio of the jet orifice diameter to the body diameter ($D=d_b/d_j$) is 12.5, and the total jet temperature $T_{0j}$ is 900 K.

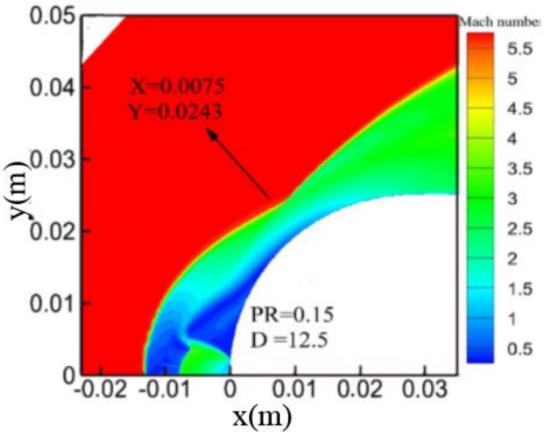
Figure 5 shows the Mach number contours at injection pressure ratios ($PR = P_{jet}/P_\infty$) of 0.075, 0.1, 0.15, 0.2, and 0.25 .According to Figure 5a, the Mach number contours at a jet pressure ratio (PR) of 0.075 cause local disturbance in the flow, creating a region with lower Mach numbers around the injection point. This effect is relatively small due to the low pressure ratio. In Figure 5b, with an increased injection pressure (PR=0.1), the disturbance in the flow is slightly more significant than PR = 0.075. The region affected by the jet expands, and a more noticeable reduction in Mach numbers around the injection point is observed. Figure 5c with PR=0.15 shows a further increase in the jet's impact on the flow. In this figure, the region with lower Mach numbers enlarges, indicating stronger interaction between the jet and the supersonic flow. Figure 5d shows a greater effect of the high-pressure jet on the flow, with the region of low Mach numbers expanding. In Figure 5e, with PR = 0.25, the most significant disturbance in the flow is observed, and the region with lower Mach numbers has the largest area among all the charts. Therefore, as the jet pressure ratio increases from 0.075 to 0.25, the disturbance in the Mach number contours increases, creating larger regions of lower Mach numbers around the injection point.



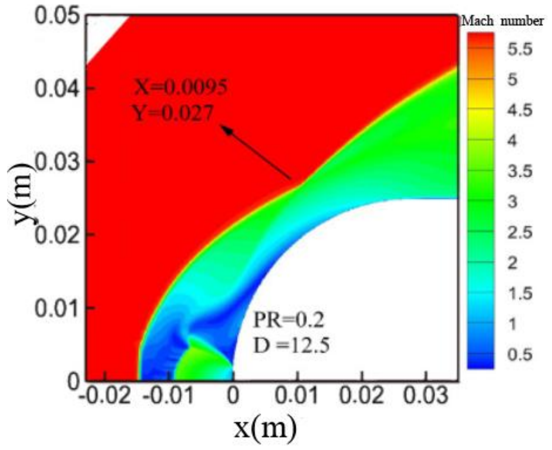
a)Jet Injection with Pressure Ratio 0.075



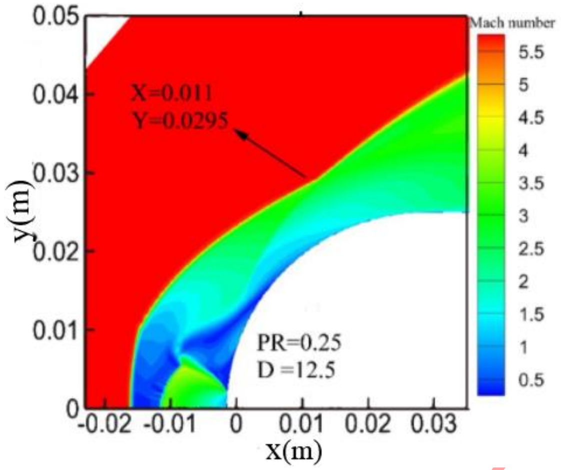
b) Jet Injection with Pressure Ratio 0.1



c) Jet Injection with Pressure Ratio 0.15



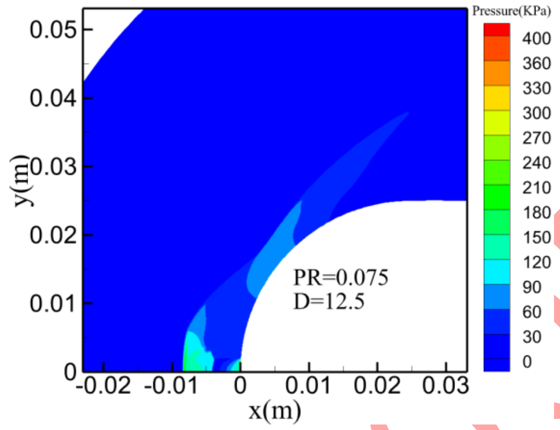

d)Jet Injection with Pressure Ratio 0.2



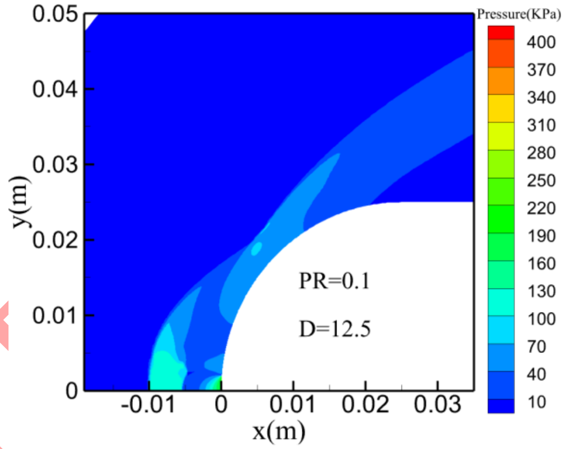

e) Jet Injection with Pressure Ratio 0.25

**Fig. 5**. Variations in Mach Number Contours at Injection Pressure Ratios of 0.075, 0.1, 0.15, 0.2, and 0.25

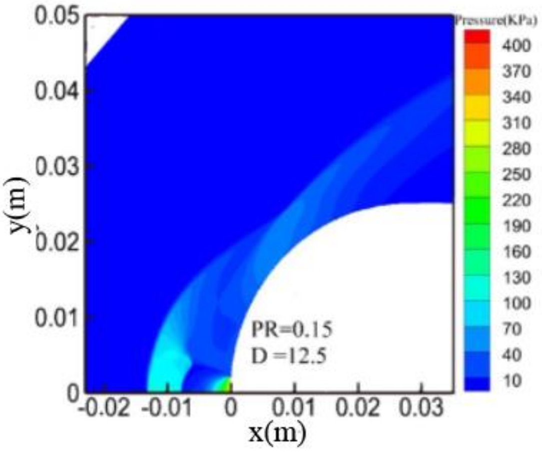
Figure 6 shows that with an increase in jet pressure ratio (PR) from 0.075 to 0.25, the static pressure contours around the nose display higher pressure regions and greater pressure gradients, indicating stronger interactions between the jet and the incoming flow with a Mach number of 6. At low PR values, the jet's influence is minimal, leading to small disturbances and a shock wave close to the cone surface. As PR increases, the high-pressure region expands and the shock wave moves further away from the cone. The highest jet pressure ratio, PR=0.25 exhibits the most significant disturbance in the flow field, marked by a large high-pressure region and high-pressure gradients. The jet's influence is dominant at this stage, significantly altering the shock wave structure and positioning it farther from the nose



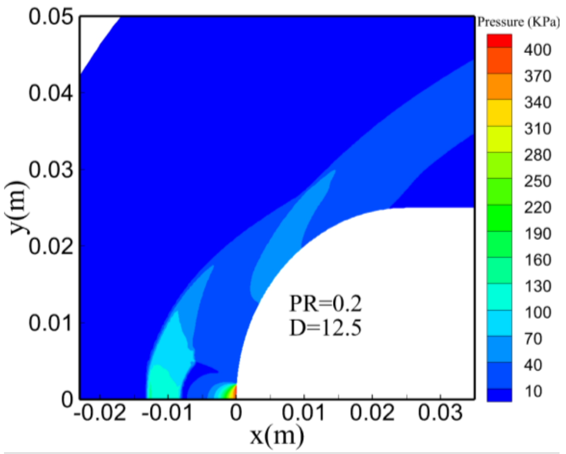

a)Jet Injection with Pressure Ratio 0.075



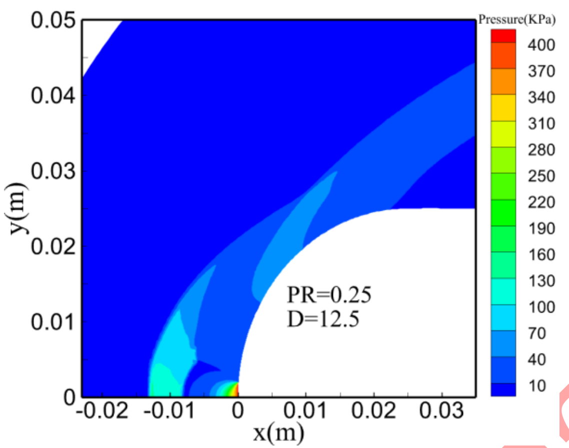

b)Jet Injection with Pressure Ratio 0.1




c)Jet Injection with Pressure Ratio 0.15



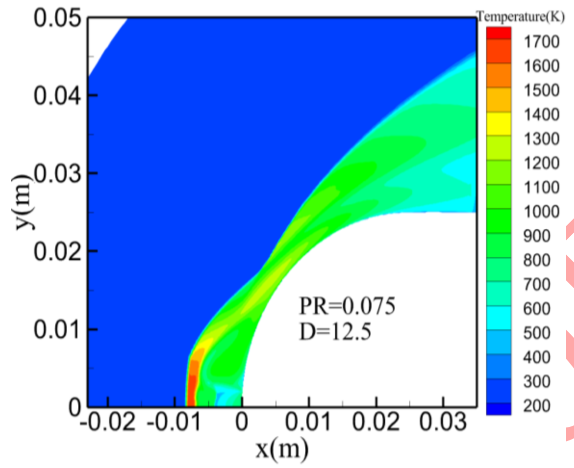

d)Jet Injection with Pressure Ratio 0.2



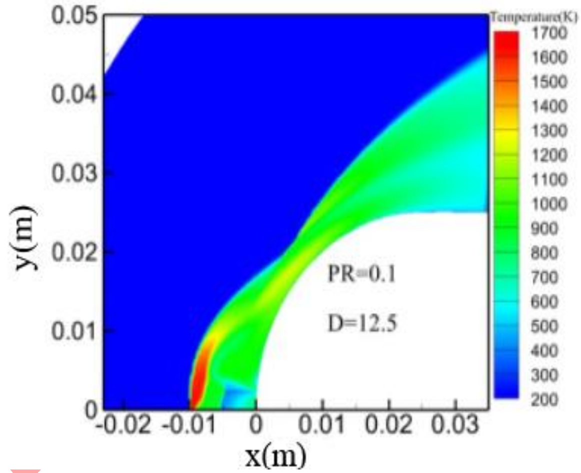

e) Jet Injection with Pressure Ratio 0.25

**Fig. 6.** Static Pressure Contours at Injection Pressure Ratios of 0.075, 0.1, 0.15, 0.2, and 0.25

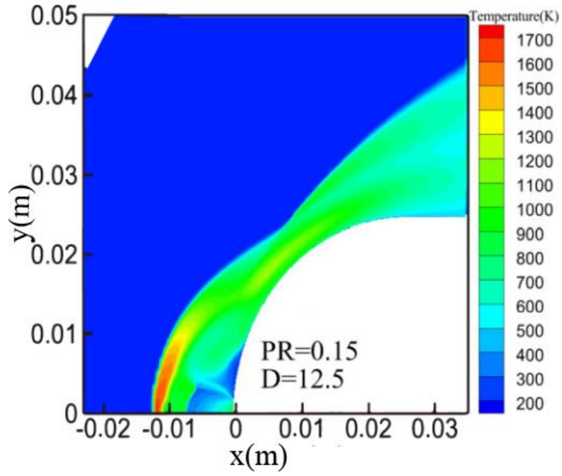
By observing the static temperature contours around the nose in Figure 7, it is seen that with an increase in jet pressure ratio (PR) from 0.075 to 0.25, the high-temperature region moves farther from the nose. Additionally, at the highest PR (0.25), it is observed that the area of the high-temperature region is the largest among all cases, indicating the bow shock moving farther away from the vehicle. Furthermore, the temperature gradient in this case is higher than in the other cases.



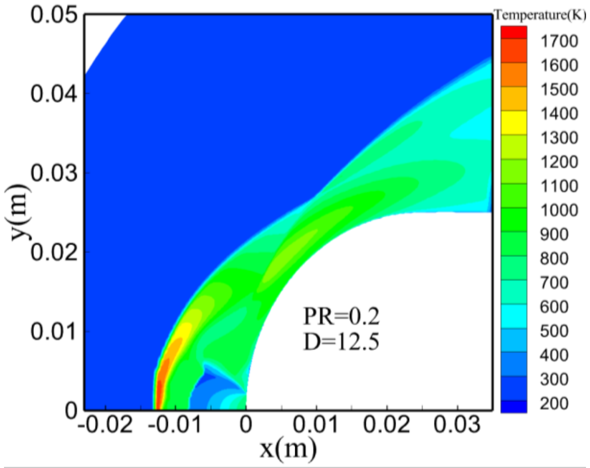

a)Jet Injection with Pressure Ratio 0.075



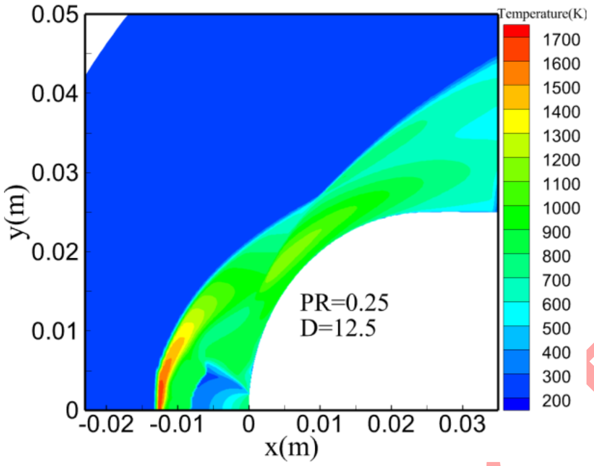

b)Jet Injection with Pressure Ratio 0.1




c)Jet Injection with Pressure Ratio 0.15




d) Jet Injection with Pressure Ratio 0.2




e) Jet Injection with Pressure Ratio 0.25

**Fig. 7.** Static Temperature Contours at Injection Pressure Ratios of 0.075, 0.1, 0.15, 0.2, and 0.25

Figure 8 shows the pressure variations on the body as a function of angle. It is observed that with an increase in the jet injection pressure ratio, the angle of the reattachment point of the flow to the body changes. In this case, the reattachment point angle changes from 37.5 to 39.2 degrees with an increase in pressure ratio. Moreover, according to Figures 8 and 9, the pressure and temperature at the reattachment point decrease with an increase in jet injection pressure ratio.

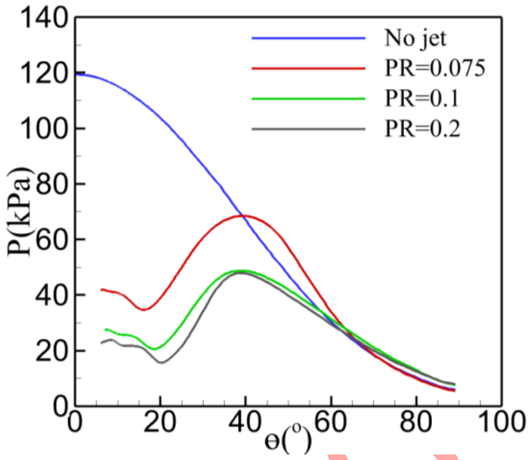



**Fig. 8.** Pressure Distribution on the Surface of the Geometry at Various Jet Injection Pressure Ratios

Based on the results of Figure 8, two phenomena can be stated. The first is that with an increase in jet injection pressure, the pressure in the upstream region of the injection point decreases. The second is that the pressure distribution after the flow reattachment point changes at higher injection pressure ratios compared to the case without injection. The high angle of the geometry in the figure above indicates that an increase in jet injection pressure significantly reduces the pressure in the front areas of the body but slightly increases the pressure in the rear areas of the geometry. Since the drag coefficient is highly dependent on the pressure in the front areas of the body, it is expected that an increase in jet injection pressure will reduce the drag coefficient. According to Figure 9, with an increase in jet injection pressure, the Stanton number decreases. A decrease in the Stanton number means that heat transfer between the wall and the fluid is reduced. In other words, the wall temperature is lower compared to the case without injection. Additionally, the angle at which the maximum Stanton number occurs decreases. This means that cooling is increased over a larger length of the nose.

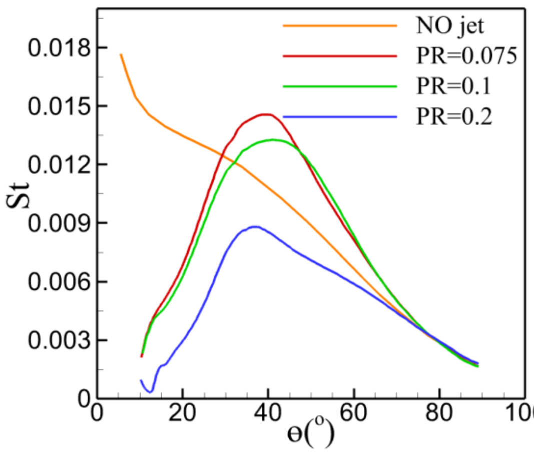



**Fig. 9**. Distribution of Stanton Number on the Surface of the Geometry at Various Jet Injection Pressure Ratios

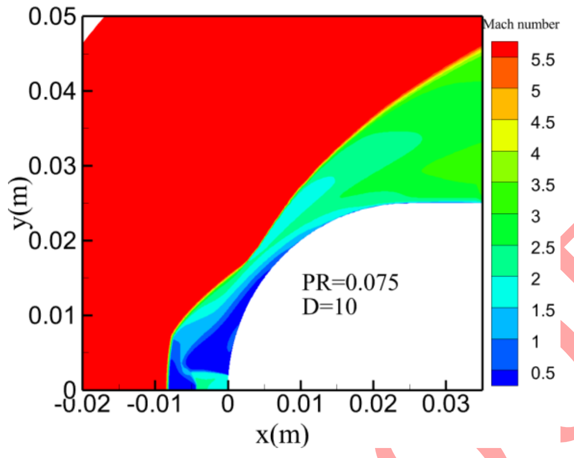
Table 3 presents the results of the drag coefficient, percentage reduction, heat transfer rate, and mass flow rate of the jet injection at various injection pressures. It is observed that the increase in injection pressure has been able to reduce the drag coefficient by 49.2%.

**Table 3.** Drag coefficient, heat transfer, and mass flow rate increase with the rise in jet injection pressure.

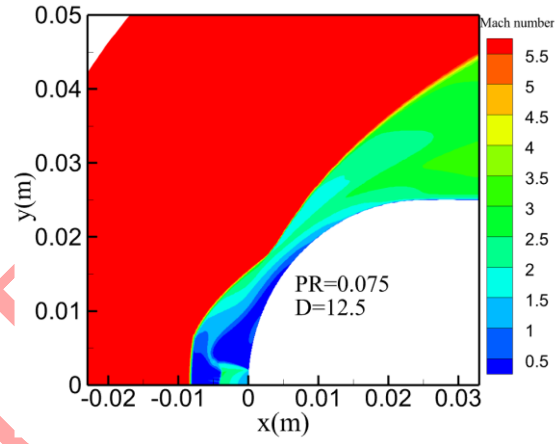
| Injection Press. (kPa) | (PR) | $C_D$ | $C_D$ Reduction (%) | H( kW/m²) | $\dot{m}_j\,(kg/s)$ |
|---|---|---|---|---|---|
| 0 (benchmark) | 0 | 0.8902 | --- | 4.48 | 0 |
| 301.5 | 0.075 | 0.7299 | 18 | 3.0458 | 0.0048 |
| 402 | 0.1 | 0.6761 | 24 | 2.9577 | 0.0064 |
| 603 | 0.15 | 0.5511 | 38 | 2.1236 | 0.0096 |
| 804 | 0.2 | 0.4928 | 44.7 | 2.0079 | 0.0129 |
| 1005 | 0.25 | 0.4518 | 49.2 | 1.7915 | 0.0161 |

### *4.2. Jet Injection Diameter Investigation*

To investigate the effect of the injection hole diameter, the jet injection pressure is considered to be 301.5 kPa, and the free stream Mach number is 6. Only the effect of changing the jet hole diameter with ratios of 10 and 12.5 is examined. In Figure 10, the Mach number distribution contour for the two simulated cases with diameter ratios of 10 and 12.5 is shown. With the increase in jet injection diameter, the area affected by the injection becomes larger, and the interaction between the curved shock wave and the reflected shock wave from the surface is not formed. Additionally, this increase in diameter results in a higher mass flow rate of the jet injection, leading to a greater distance of the curved shock wave from the surface.




a) Pressure Ratio 0.075 and D=10




b)Pressure Ratio 0.075 and D=12.5

**Fig. 10**. Mach Number Contour at Injection Diameter Ratios of 10 and 12.5

Figure 11 shows the pressure distribution on the surface as a function of angle. It is observed that the maximum pressure for the case with an injection diameter ratio of 12.5 is 78.21 kPa, and for the case with an injection diameter ratio of 10, it is 71.7 kPa. Additionally, the increase in injection diameter causes the maximum pressure to occur at smaller angles on the surface, such that for the ratio of 12.5, the maximum pressure occurs at an angle of 36.5 degrees, and for the ratio of 10, it occurs at an angle of 38.2 degrees. This indicates that an increase in diameter leads to a more uniform distribution of pressure on the surface.

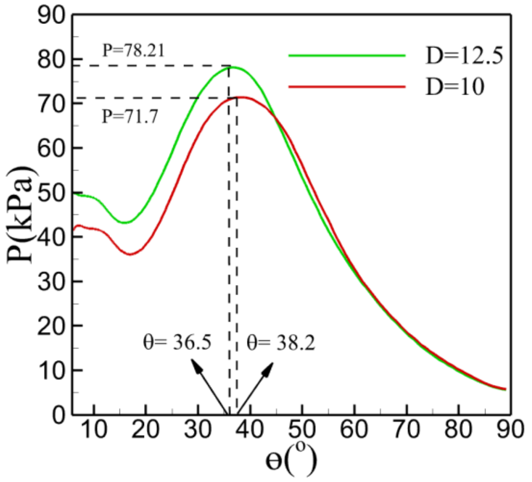
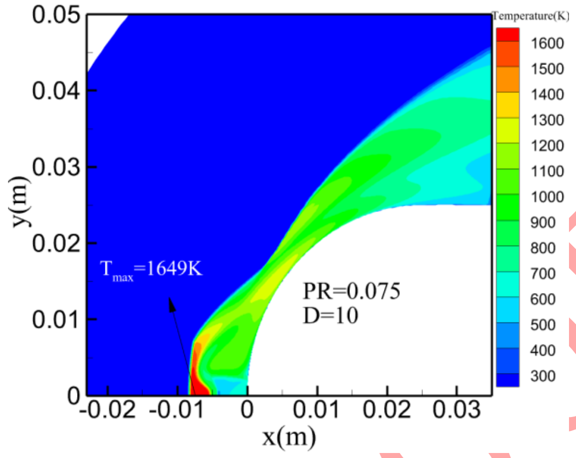



**Fig. 11**. Static Pressure Distribution on the Surface of the Body at Diameter Ratios of 10 and 12.5

The temperature contours for the two diameter ratios of 10 and 12.5 are depicted in Figure 12. The maximum temperature for the cases with injection diameter ratios of 10 and 12.5 are 1649 K and 1644 K, respectively. Additionally, the x-coordinates of these maximum temperature points for the injection diameters of 10 and 12.5 are -0.006 m and -0.0074 m, respectively. It is observed that the higher injection diameter results in a reduction of the maximum temperature within the solution domain.



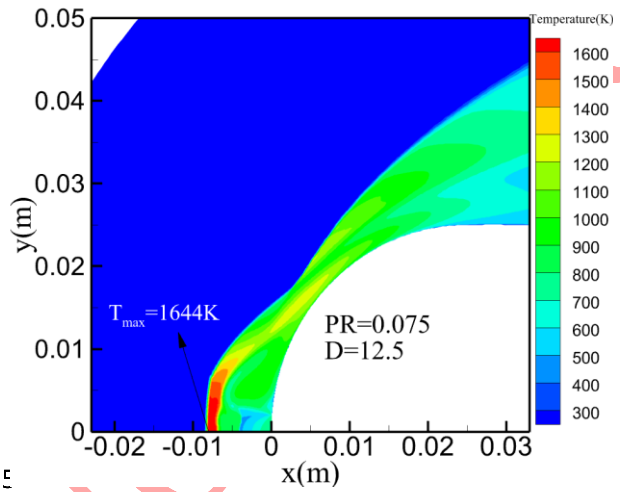




**Fig. 12.** Static Temperature Contour at Injection Diameter Ratios of 10 and 12.5

According to Figure 13, the maximum Stanton number for diameter ratios of 10 and 12.5 is 0.011 and 0.0145, respectively. It is observed that with an increase in injection diameter, the Stanton number decreases. This means that wall heat transfer is reduced, and due to the constant free stream air temperature, the wall temperature consequently decreases. Therefore, an increase in jet diameter leads to a reduction in wall temperature.

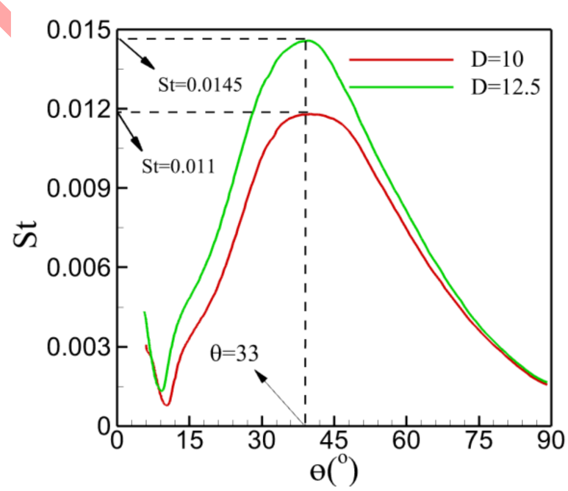



**Fig. 13.** Distribution of Stanton Number at Injection Diameter Ratios of 10 and 12.5

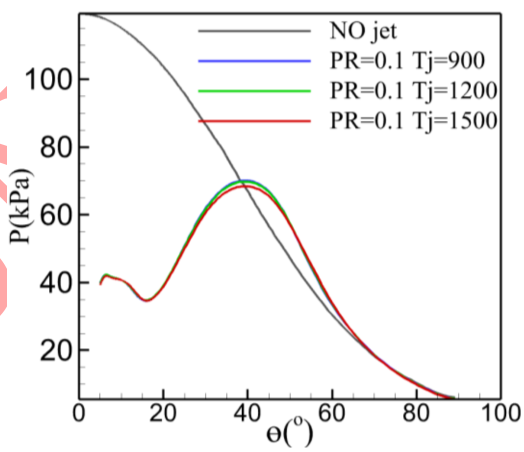
Table 4 shows that the drag coefficient decreases with an increase in jet hole diameter. It is also observed that with an increase in the mass flow rate of the jet injection, both the drag coefficient and heat transfer decrease. However, providing this high mass flow rate for a long period requires very large equipment and space. Therefore, beyond a certain point, increasing the mass flow rate is not feasible for practical use.

**Table 4.** Results of Drag Coefficient and Percentage Reduction with Increasing Jet Hole Diameter

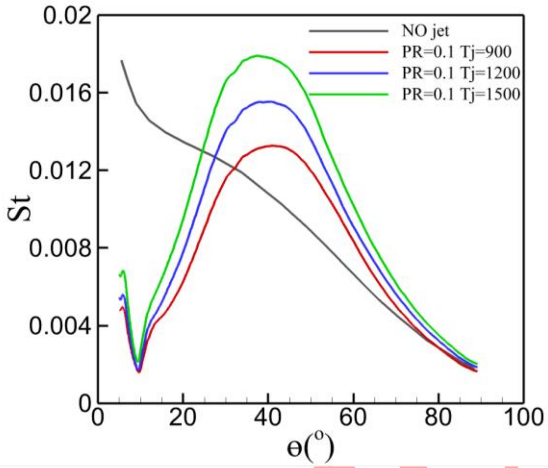
| $d_j(mm)$ | D(Dia. Ratio) | $C_D$ | $C_D$ Reduction (%) | H (kW/m²) | $\dot{m}_j(kg/s)$ |
|---|---|---|---|---|---|
| 0 | --- | 0.89 | --- | 4.48 | --- |
| 4 | 12.5 | 0.73 | 18 | 3.0458 | 0.0048 |
| 5 | 10 | 0.68 | 23 | 2.6546 | 0.0075 |

### *4.3. Investigation of Injection Jet Temperature*

Three jet injection temperatures of 900 K, 1200 K, and 1500 K were considered. In all these temperatures, the injection pressure ratio is 0.1 and the diameter ratio is 12.5. Based on the simulation results, the distribution of static pressure and the Stanton number on the geometry surface are shown in Figure 14. According to Figure 14-a, it is observed that with an increase in jet temperature at a constant pressure ratio, the pressure distribution on the surface does not change significantly. Only in the reattachment region is there a slight increase in pressure, which is negligible. Therefore, it can be concluded that changing the jet temperature has little effect on the pressure distribution on the surface and consequently on the drag coefficient. Table 7 presents the results of the drag coefficient and percentage changes with the increase in jet injection temperature, which confirms the negligible changes in drag with jet temperature. Figure 14-b shows the variations in the Stanton number on the surface of the nose. It is observed that the lower the jet injection temperature, the lower the Stanton number. This means that jet injection at a lower temperature leads to improved cooling of the nose. Additionally, quantitatively, the heat flux values for jet injection at different temperatures are mentioned in Table 5.




a)Pressure Variations




b)Stanton Number Variations

**Fig. 14**. Variations in Pressure and Stanton Number on the Surface of the Nose at Injection Temperatures of 900 K, 1200 K, and 1500 K

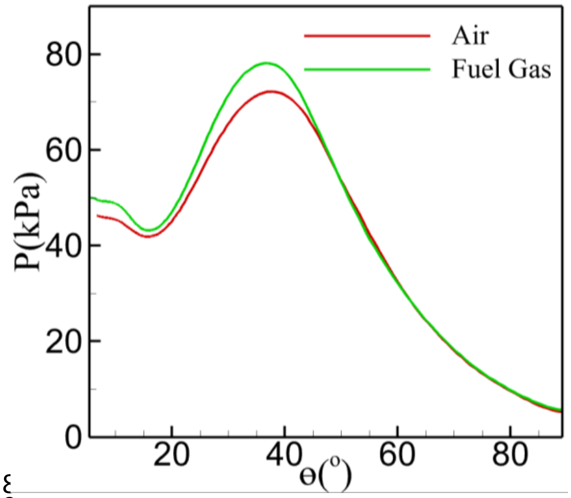
**Table 5.** Results of Drag Coefficient and Percentage Reduction with Increasing Stagnation Temperature of Jet Injection

| $T_{0,j}(K)$ | $C_D$ | $C_D$ Reduction (%) | H (kW/m²) | $\dot{m}_j(kg/s)$ |
|---|---|---|---|---|
| 0 | 0.89 | --- | 4.48 | --- |
| 900 | 0.6762 | 24 | 2.96 | 0.0064 |
| 1200 | 0.6842 | 23 | 3.4 | 0.0055 |
| 1500 | 0.6837 | 23.2 | 3.86 | 0.0049 |

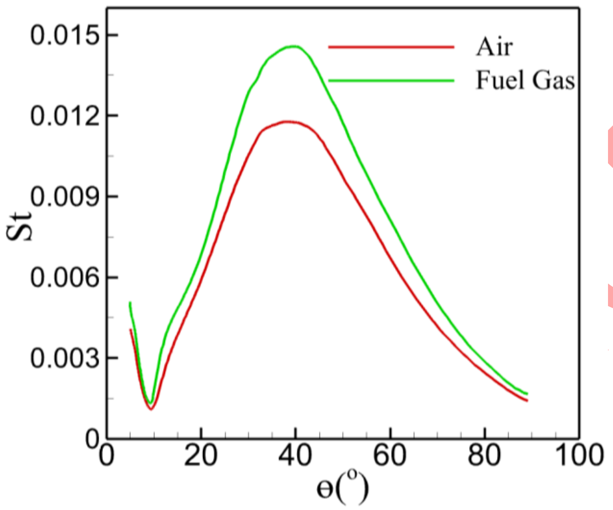
### *4.4. Investigation of the Injected Fluid Material*

Another important parameter in the issue of drag reduction using jet injection is the type of injected fluid. Changing the fluid properties alters certain physical behaviors, such as the penetration and dispersion of the injected fluid. Accordingly, the effects of two injection fluids, air and a composite gas or fuel gas ($N_2O$), will be examined. This study is conducted at a pressure ratio of 0.075, a jet temperature of 900 K, and a diameter ratio of 12.5. In Figure 15-a, the pressure distribution for the two injection fluids is shown. The pressure on the surface from the jet injection area to before the reattachment point is lower with air injection compared to the composite gas case; such that at the angle of maximum surface pressure, 37.5 degrees, air injection achieves 7.5% less pressure than composite gas injection.

The results of the Stanton number distribution on the surface for these two different fluids are shown in Figure 15-b. By changing the injection fluid from composite gas to air, the Stanton number at its maximum value decreases by approximately 19.3%. Unlike the static pressure distribution, where the pressure of the two fluids equalizes downstream of the maximum pressure point, the Stanton number is higher for the composite gas than for the injected air. In other words, changing the injection fluid affects the overall surface heat transfer but only changes the surface pressure up to the maximum surface pressure area and slightly downstream of it.




a) Pressure Distribution on the Surface of the Nose




b) Distribution of Stanton Number on the Surface of the Nose

**Fig. 15**: Variations in Pressure and Stanton Number for the Injection of Two Different Fluids

### *4.5. Double Cone Geometry Without Jet Injection*

The innovation of this paper lies in considering a double cone geometry for the nose. The studied geometry along with its dimensions is presented in Figure 16.

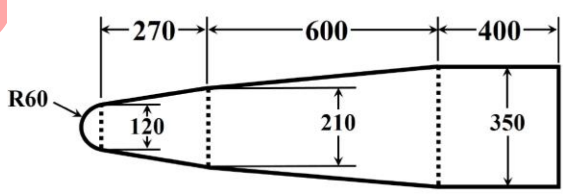



**Fig. 16.** Double Cone Geometry (Dimensions are in Millimeters)

For the numerical simulation of the double cone geometry, a structured grid is used. The numerical simulation of this geometry is also performed using Fluent software, with the previous general settings and the far-field flow conditions according to Table 6.

**Table 6.** Far-Field Flow Conditions for Double Cone Geometry

| | |
|---|---|
| Freestream Mach Number | 4.5 |
| Freestream Static Pressure (kPa) | 41.06 |
| Freestream Static Temperature (K) | 242 |

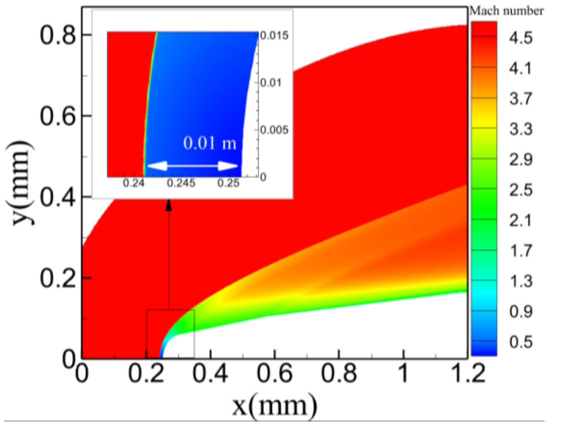
Accordingly, the stagnation pressure and temperature in the freestream are calculated to be approximately 1091 bar and 1220 K, respectively. The independence of the structured computational grid in the absence of jet injection was examined in three grids with 182,000, 282,000, and 370,000 cells. The results of the drag coefficient and surface heat transfer for these three grids are shown in Table 7.

**Table 7.** Grid Independence Results for Double Cone Geometry

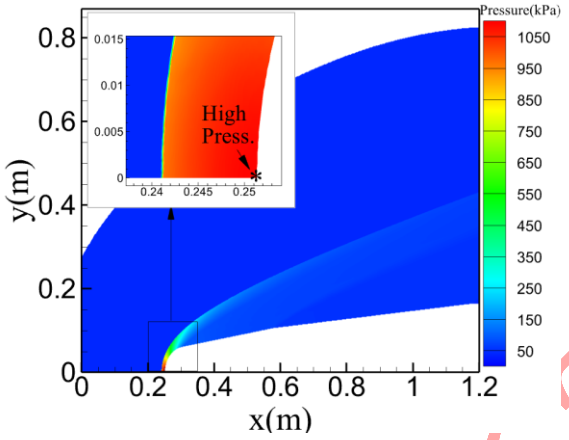
| # | No. grid | $C_D$ | H (kW/m²) |
|---|---|---|---|
| **Coarse** | 182380 | 0.1666 | 506311 |
| **Standard** | 282660 | 0.1679 | 542372 |
| **fine** | 370150 | 0.1680 | 540687 |

Based on the results of Table 7, the changes in the drag coefficient and surface heat flux from the standard grid compared to the fine grid are 0.06% and 0.31%, respectively. The change in the drag coefficient in the coarse grid is approximately 0.7%, which is acceptable, but due to the 1.7% change in heat flux, the standard grid is used as the reference grid in the rest of the article.

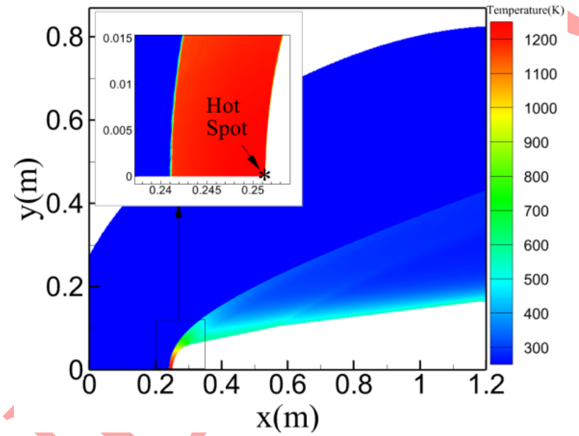
The contours of the Mach number, static pressure, and static temperature are shown in Figure 18.




a) Mach Number Contour in Double Cone Geometry Without Jet Injection




b) Static Pressure Contour in Double Cone Geometry Without Jet Injection



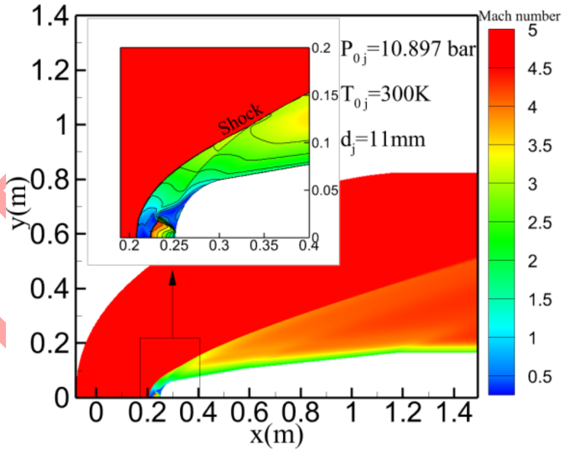

c)Temperature Contour in Cone Geometry Without Jet Injection

**Fig. 17**.Static Temperature Contour in Double Cone Geometry Without Jet Injection

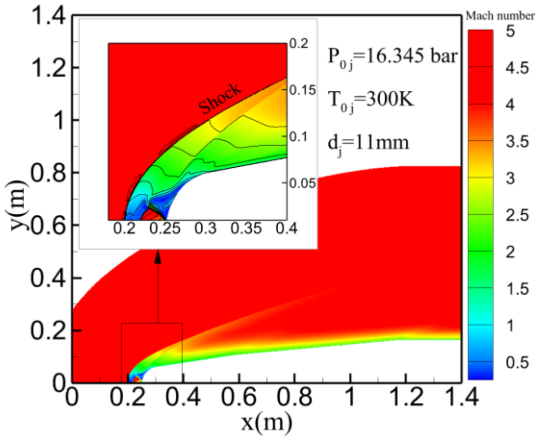
Considering the contours presented for the case without jet injection, it is observed that the most significant changes occur at the front of the nose. According to Figure 18-a, the minimum distance of the bow shock from the nose is equal to 10 millimeters. Additionally, Figure 18-b shows that the maximum pressure value is 1091 kilopascals and occurs at the stagnation point in the center of the nose. Figure 18-c also shows the maximum temperature at the stagnation point on the nose, and its value is 1225 K.

### *4.6. Investigation of the Effect of Jet Pressure Ratio in Double Cone Geometry*

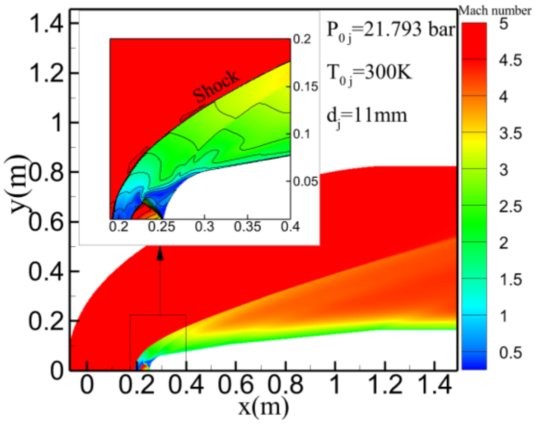
To investigate the effect of the jet injection pressure parameter on drag and heat reduction in this geometry using numerical simulation, three values of 10.897, 16.345, and 21.793 bar at a jet hole diameter of 11 millimeters are examined. Considering the freestream stagnation pressure (i.e., 118.5 bar), the three dimensionless injection pressure ratios are 0.092, 0.138, and 0.184, respectively, similar to the values studied in the hemispherical geometry (Figure 19). For the three aforementioned pressure ratios, the bow shock forms at distances of 44, 52, and 59 millimeters.




a) Injection Pressure Ratio 0.092




b) Injection Pressure Ratio 0.138




c) Injection Pressure Ratio 0.184

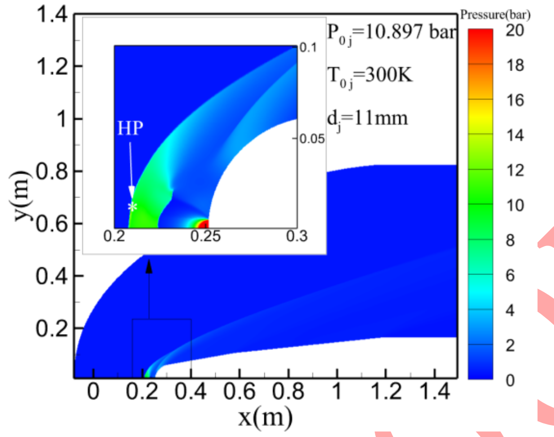
**Fig. 18**. Mach Number Contour in Double Cone Geometry for Various Jet Injection Pressures

The values of the drag coefficient and heat flux are presented in Table 8. The results show that increasing the injection pressure for the double cone geometry leads to a reduction in the drag coefficient. At an injection pressure ratio of 0.184, the drag coefficient is reduced by 62.7% compared to the baseline case (without injection). Additionally, the heat transfer rate also decreases at an injection pressure ratio of 0.184, indicating that increasing the injection pressure leads to more effective cooling of the nose.

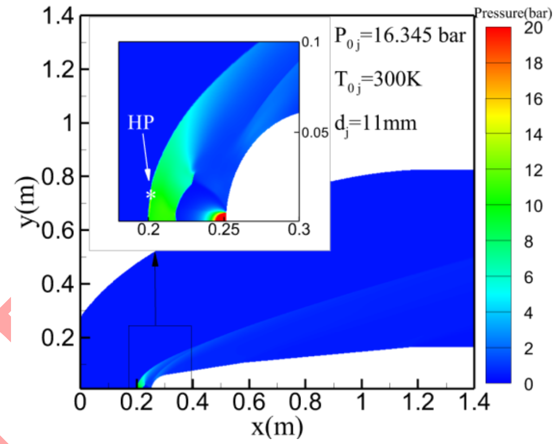
**Table 8.** Change in Drag Coefficient and Heat Flux of Double Cone Geometry with Increased Jet Injection Pressure

| Injection Press. (kPa) | (PR) | $C_D$ | $C_D$ Reduction (%) | H( kW/m²) | $\dot{m}_j (kg/s)$ |
|---|---|---|---|---|---|
| 0 (benchmark) | 0 | 0.1679 | --- | 842.372 | 0 |
| 10.89 | 0.092 | 0.0865 | 48.5 | 412.708 | 2.33 |
| 16.34 | 0.138 | 0.071 | 57.7 | 406.974 | 3.49 |
| 21.79 | 0.184 | 0.0627 | 62.7 | 318.040 | 4.66 |

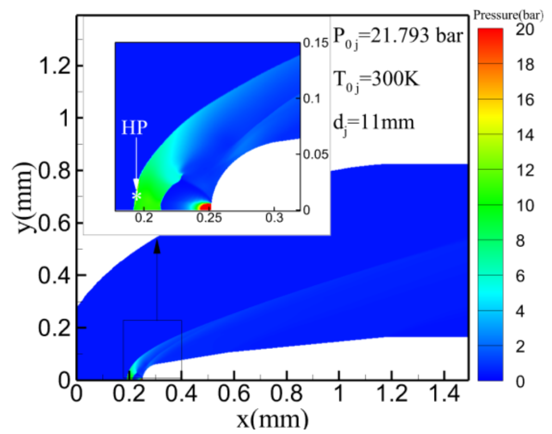
In Figure 18, it can be seen that with the increase in jet injection pressure, the recompression wave generated by the injection combines with the curved shock wave of the geometry, and the pressure at the reattachment point decreases. The maximum static pressure after the shock, in the case of an injection pressure of 10.897 bar, is 14.28 bar. Also, for the injection pressure of 16.345 bar, the pressure after the shock is 14.70 bar, and for the injection pressure of 21.793 bar, it is 15.62 bar.




a) Static Pressure Contour at 10.897 Bar Jet Injection Pressure




b) Static Pressure Contour at 16.345 Bar Jet Injection Pressure




c) Static Pressure Contour at 21.793 Bar Jet Injection Pressure

**Fig. 19**. Static pressure Contour in Double Cone Geometry for Various Jet Injection Pressures

With the increase in injection pressure, it is expected that the temperature around the nose of the geometry will decrease. Figure 19 clearly shows that with the increase in the injection pressure ratio, the area of the cold region resulting from the injection becomes larger. However, it should be noted that with the increase in jet injection pressure, the temperature after the shock, which is the region with the highest temperature, for injection pressures of 10.897, 16.345, and 21.793 bar is 1160.2 K, 1159.4 K, and 1153.5 K, respectively.

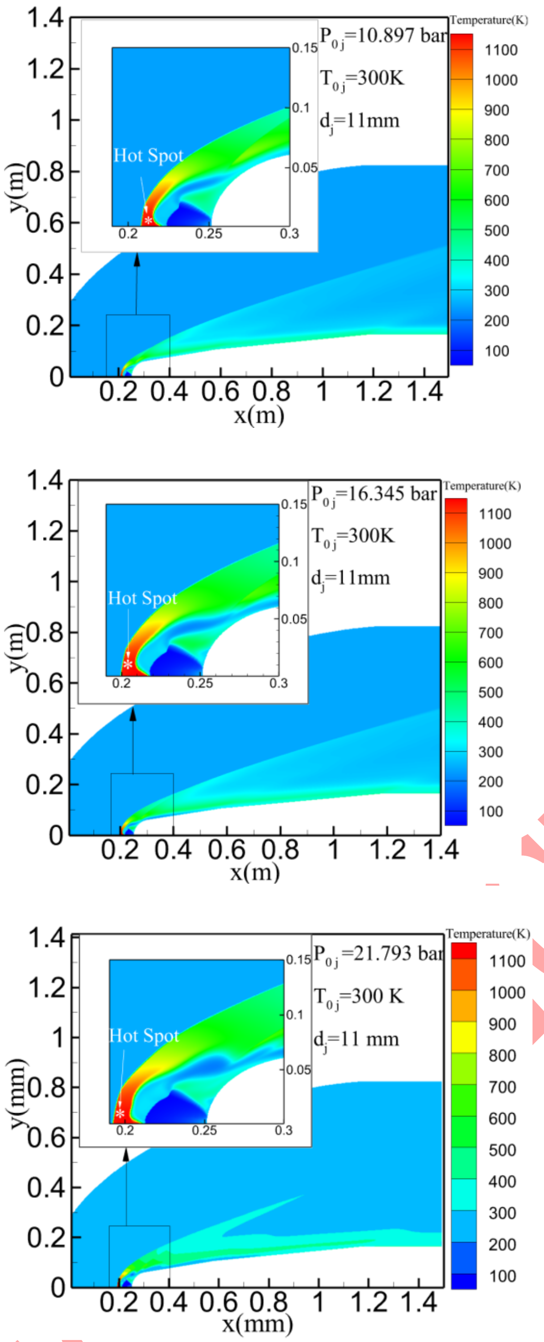



**Fig. 20.** Static Temperature Contour in Double Cone Geometry for Various Jet Injection Pressures

### *4.7. Investigation of the Effect of Jet Diameter in Double Cone Geometry*

To investigate the effect of jet injection diameter in this geometry, simulations were evaluated for three diameters: 11 mm, 13.2 mm, and 16.5 mm at an injection pressure of 21.79 bar. According to Table 9, as the jet injection diameter increases, the drag coefficient decreases and the mass flow rate increases. The percentage reduction in drag coefficient for the sample with the largest jet injection diameter is 75.04%, which is a significant value.

**Table 9.** Results of Changes in Drag Coefficient and Heat Flux of Double Cone Geometry with Increased Jet Hole Diameter

| $d_j(mm)$ | D(Dia. Ratio) | $C_D$ | $C_D$ Reduction (%) | H (kW/m²) | $\dot{m}_j(kg/s)$ |
|---|---|---|---|---|---|
| 0 | --- | 0.1679 | --- | 542.372 | --- |
| 16.5 | 20 | 0.0419 | 75.04 | 308.468 | 10.485 |
| 13.2 | 25 | 0.0522 | 68.9 | 290.444 | 6.71 |
| 11 | 30 | 0.0627 | 62.7 | 318.040 | 4.66 |

In Figure 20, the Mach number contour for three different jet diameter ratios is presented. According to the obtained results, the distances of the curved shock wave in front of the geometry for increasing jet hole diameters are 58, 69, and 78 millimeters, respectively; this indicates that the wave moves further away from the nose of the geometry as the jet hole diameter increases. Additionally, by comparing Table 8 and Table 9, it is observed that with an increase in mass flow rate from approximately 2.3 to 4.6 kilograms per second (increased injection pressure), the percentage reduction in the drag coefficient changes by 14 units (from 48 to 62). However, with an increase in mass flow rate from 4.6 to 10.5 kilograms per second (increased injection diameter), the percentage reduction in the drag coefficient changes by 13 units (from 62 to 75). In other words, operationally, using a smaller jet hole with higher injection pressure is more efficient, as it achieves suitable drag and heat flux reduction with lower mass flow consumption.

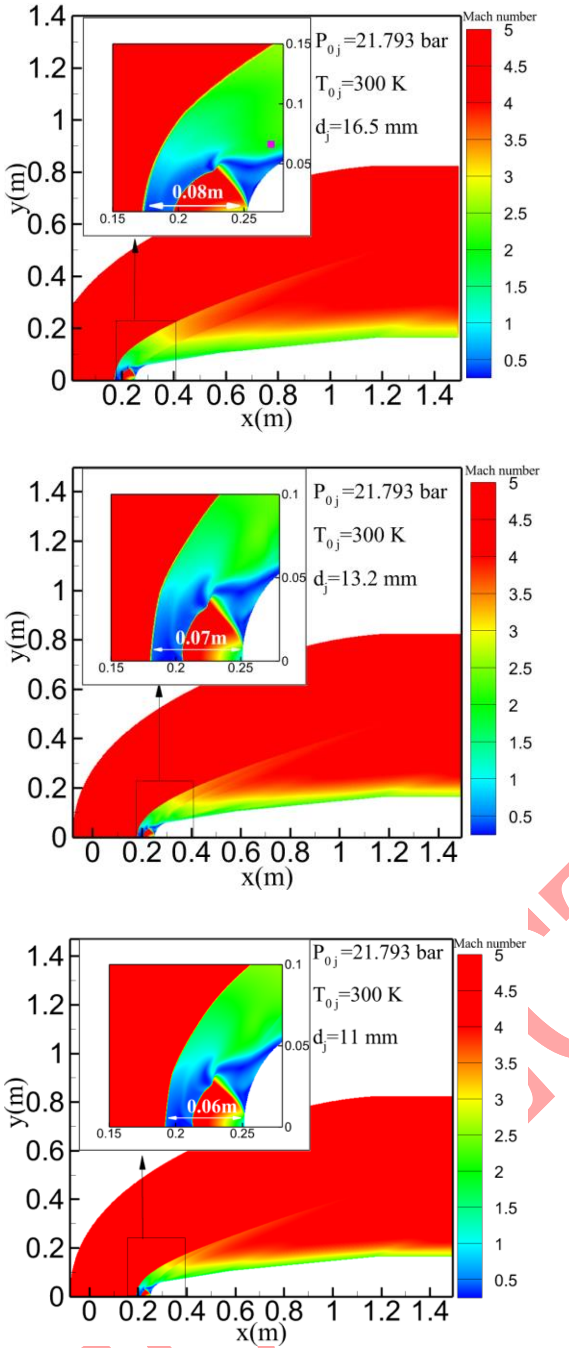



**Fig. 21.** Mach Number Contour in Double Cone Geometry for Various Jet Injection Diameters

Figure 21 shows the pressure contour for different jet injection diameters. The results indicate that the pressure after the shock formation area increases with the increase in the jet injection diameter. The pressure values for jet injection diameters of 11 mm, 13.2 mm, and 16.5 mm are 15.96 bar, 16.07 bar, and 19.3 bar, respectively. The injection pressure in all three cases is 21.793 bar. This indicates that the increase in injection pressure leads to the formation of a stronger bow shock upstream of the nose. However, at the same time, the distance of the shock from the nose increases with the increase in injection pressure.

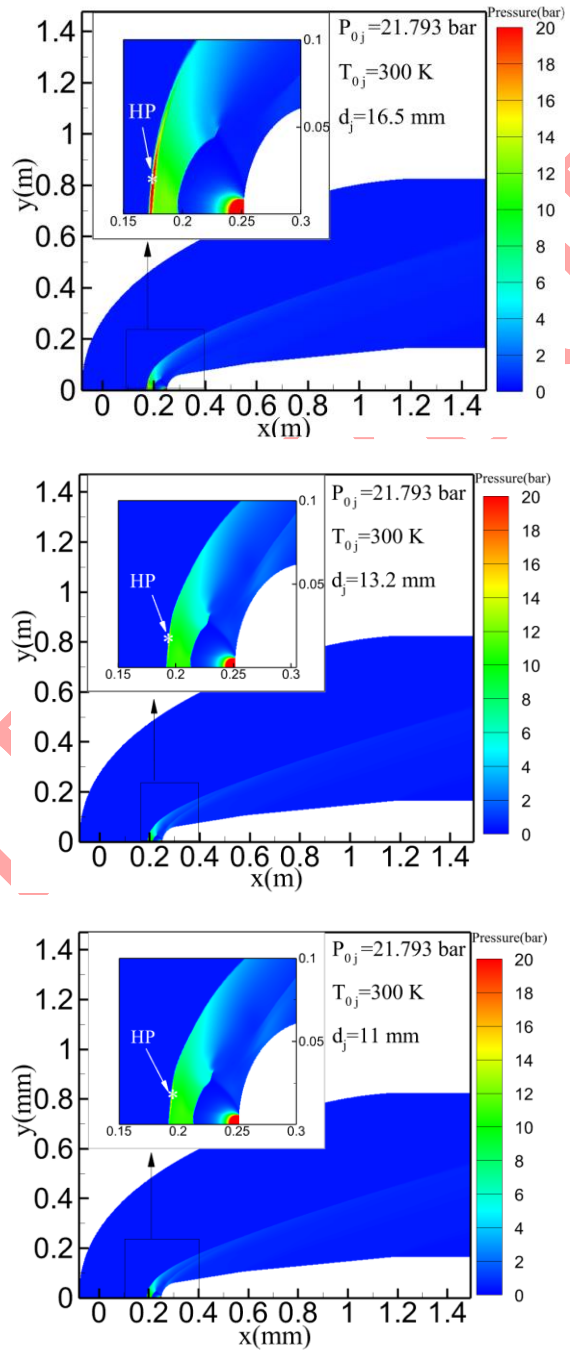



**Fig. 22.** Static Pressure Contour in Double Cone Geometry for Various Jet Injection Diameters

According to Figure 22, which shows the temperature distribution of the double cone geometry for different jet injection diameters (16.5 mm, 13.2 mm, and 11 mm), the maximum temperature values for these diameters are 1148.1 K, 1152.1 K, and 1153.9 K, respectively. Therefore, it can be concluded that with the increase in jet injection diameter, the maximum temperature at the front of the nose (shock formation area) decreases. Additionally, it should be noted that the injection temperature for all three cases is 300 K.

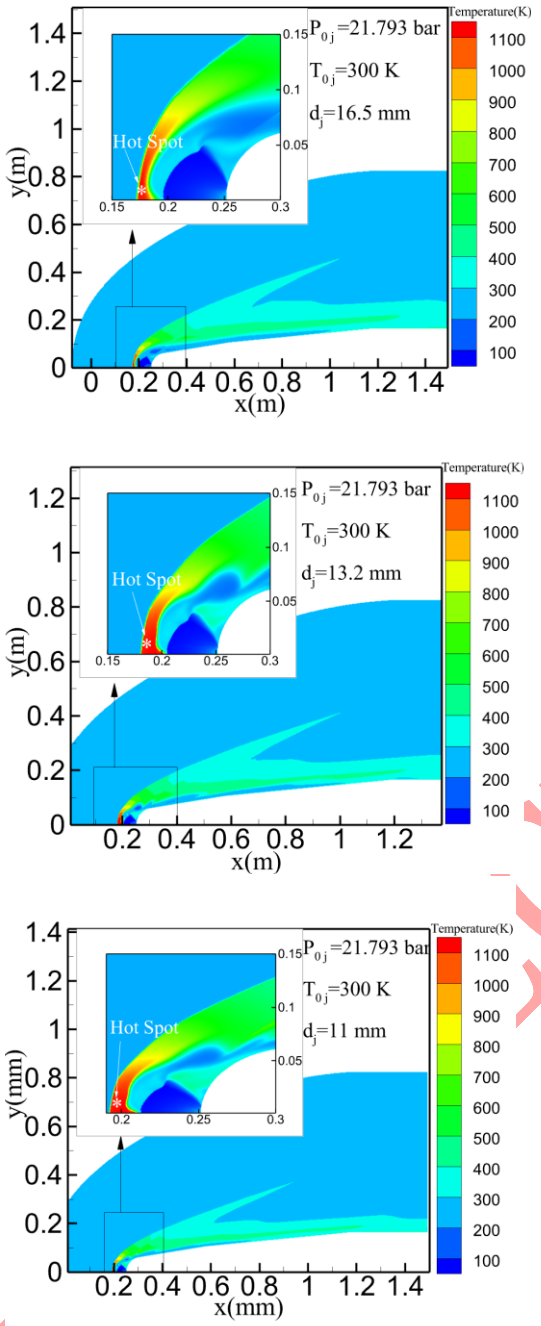



**Fig. 23**. Static Temperature Contour in Double Cone Geometry for Various Jet Injection Diameters

## 5. Conclusions

This study analyzed the effects of jet injection on drag reduction and heat transfer control for single-cone and double-cone nose geometries in hypersonic flow conditions. The results demonstrated that increasing the jet injection pressure significantly reduces aerodynamic drag, with reductions of 49.2% for the single-cone geometry and 62.7% for the double-cone geometry. Additionally, increasing the injection diameter further enhances drag reduction, reaching 75.04% for the double-cone case with a 16.5 mm injection diameter. The findings also indicate that jet injection shifts the bow shock upstream, reducing stagnation pressure and temperature, which helps in thermal management. Furthermore, using alternative injection gases, such as gas mixtures instead of air, lowered the maximum Stanton number by 19.3%, further enhancing heat transfer control. Beyond a certain injection pressure, the improvement in drag reduction becomes minimal, and the primary benefit transitions to heat reduction. The study confirms that optimizing jet injection parameters—such as pressure ratio, injection diameter, and injected fluid properties—is essential for balancing drag reduction and thermal protection in hypersonic applications. Future research can explore the combined effects of jet injection with other flow control techniques, such as aerospikes or energy discharge methods, to enhance aerodynamic efficiency further. In general The results indicate that increasing the jet injection pressure ratio is the most effective method for reducing drag, . The most effective method for reducing the Stanton number and thereby minimizing heat transfer is increasing the injection temperature, while the best approach for lowering the temperature near the device is optimizing the jet diameter and injection pressure.

While this study provides insights into the effects of jet injection on drag and heat transfer in hypersonic flows, several avenues for future research can further advance this field including: combination with other flow control Techniques, unsteady flow analysis, optimization of Injection parameters, thermal and structural analysis, alternative injection gases and mixtures, and studying and simulation of three-dimensional effects:

## Nomenclature

| | |
|---|---|
| *H* | Specific enthalpy [kJ/kg] |
| *I* | Exergy destruction rate [kJ/kg] |
| M | Mass flow rate [kg/s] |
| P | Pressure [bar] |

## Conflicts of Interest

There are no conflicts of interest for this research.

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